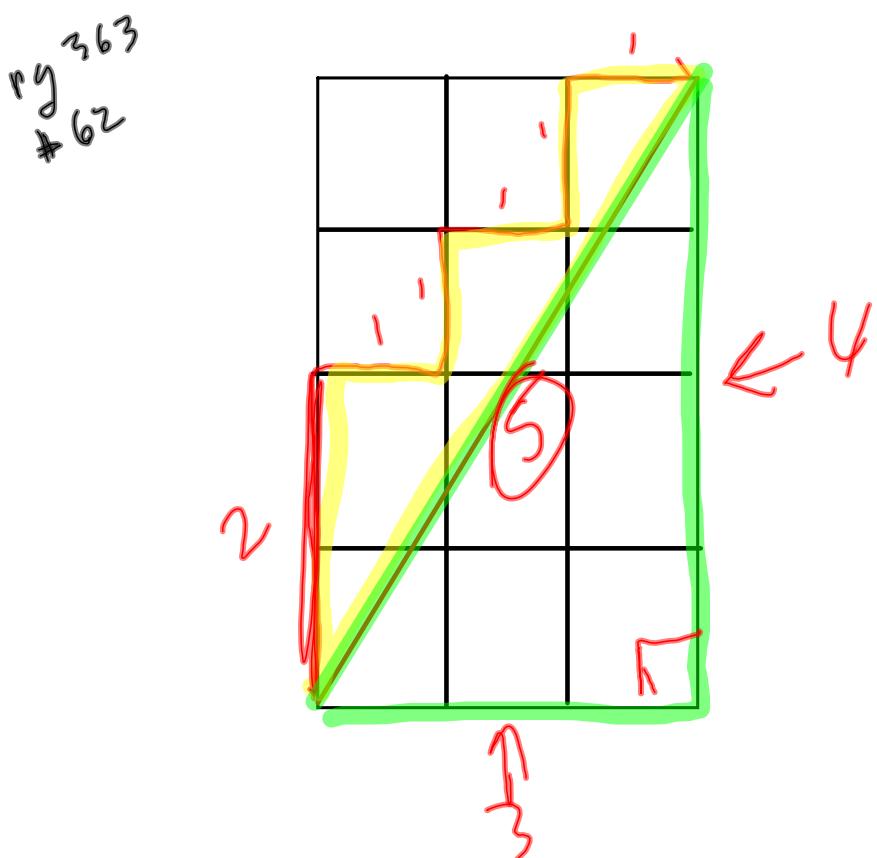
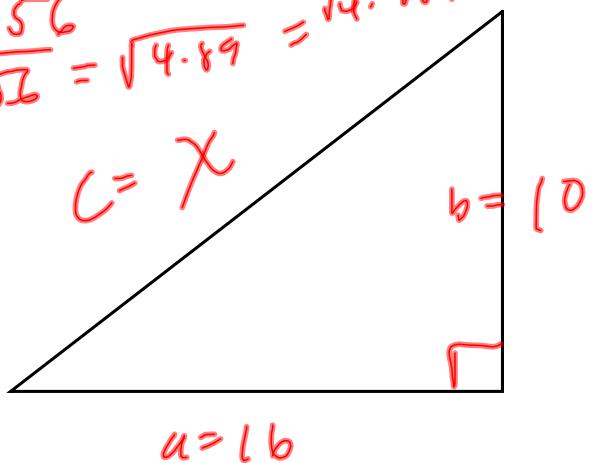


- $$\textcircled{1} \quad \sqrt{5} \cdot \sqrt{10} = \sqrt{5 \cdot 10} = \sqrt{50} = \underline{\underline{\sqrt{2 \cdot 25}}} \\ \underline{\underline{1, 4, 9, 16, 25, 36, 49, \dots}} = \sqrt{2} \cdot \sqrt{25} \\ \textcircled{11} \quad 28 \div \sqrt{8} = \frac{28}{\sqrt{8}} = \frac{28}{\sqrt{2 \cdot 4}} = \frac{28}{\sqrt{2} \cdot \sqrt{4}} = \frac{28}{2\sqrt{2}} = \frac{14}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} \\ = \frac{14\sqrt{2}}{2} = 7\sqrt{2} \\ \textcircled{12} \quad \sqrt{\frac{25}{20}} = \sqrt{\frac{5}{4}} = \frac{\sqrt{5}}{\sqrt{4}} > \frac{\sqrt{5}}{2} \\ \textcircled{13} \quad \sqrt{12} \cdot \sqrt{2} = \sqrt{12 \cdot 2} = \sqrt{24} = \sqrt{4 \cdot 6} = \sqrt{4} \cdot \sqrt{6} = 2\sqrt{6}$$



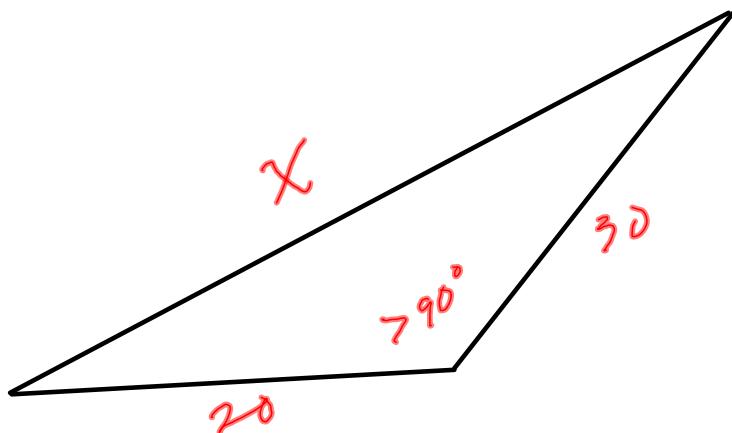
$\text{Pj } 361$   
 $\Rightarrow 13^2 + 10^2 = x^2 \quad 49, 16, 25, 36, 49, 64, 81$   
 $256 + 100 = x^2$

$$x^2 = 356 \quad x = \sqrt{356} = \sqrt{4 \cdot 89} = \sqrt{4} \cdot \sqrt{89} = 2\sqrt{89}$$



$$a=10$$

$\text{Pj } 364$   
 $\# 72$



Two special right triangles determined by  $\angle$  measures

Two special right triangles determined by  $\angle$  measures

45-45-90

Two special right triangles determined by  $\angle$  measures

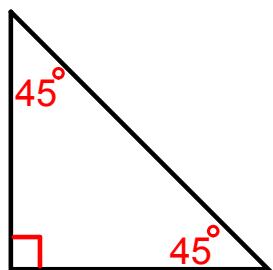
45-45-90

30-60-90

Two special right triangles determined by  $\angle$  measures

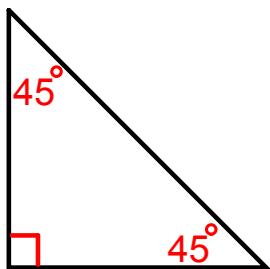
45-45-90

30-60-90

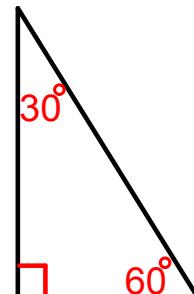


Two special right triangles determined by  $\angle$  measures

45-45-90

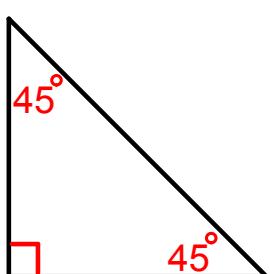


30-60-90

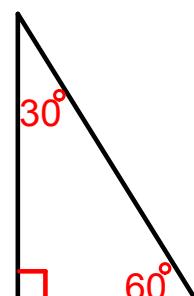


Two special right triangles determined by  $\angle$  measures

45-45-90



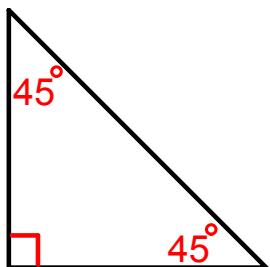
30-60-90



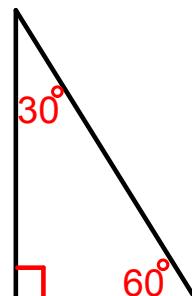
The sides of each  $\Delta$  are always in a specific ratio...

## Two special right triangles determined by $\angle$ measures

45-45-90



30-60-90

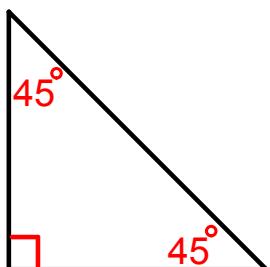


The sides of each  $\Delta$  are always in a specific ratio...

Your task is to figure out the side ratio for each  $\Delta$ .

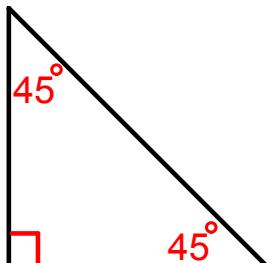
## Side length ratios for a 45-45-90 $\Delta$

45-45-90



## Side length ratios for a 45-45-90 $\Delta$

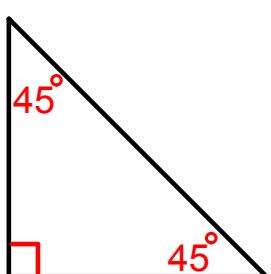
45-45-90



Hints...

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

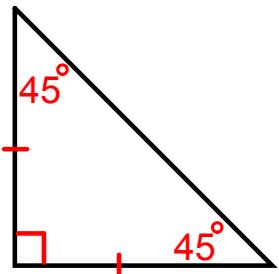


Hints...

- Give shortest side a convenient length

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

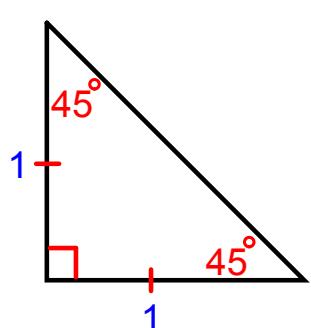


Hints...

- Give shortest side a convenient length

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

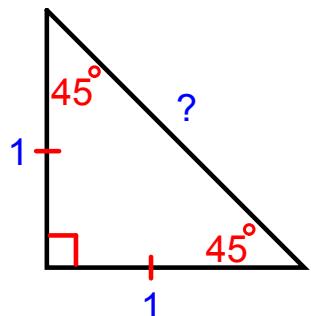


Hints...

- Give shortest side a convenient length

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

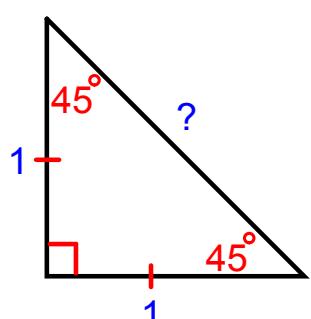


Hints...

- Give shortest side a convenient length

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

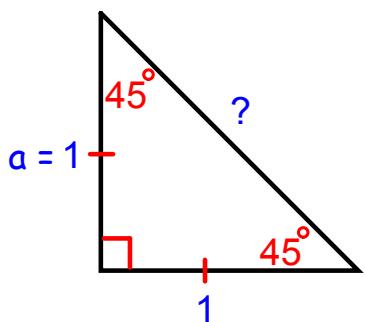


Hints...

- Give shortest side a convenient length
- Use Pythag Thm

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

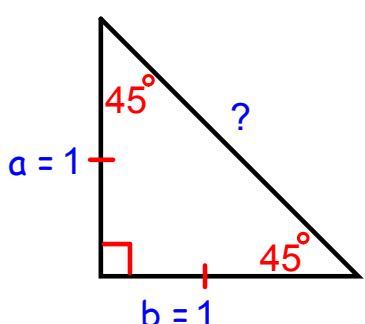


Hints...

- Give shortest side a convenient length
- Use Pythag Thm

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

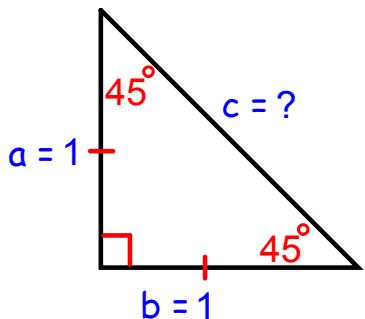


Hints...

- Give shortest side a convenient length
- Use Pythag Thm

## Side length ratios for a 45-45-90 $\Delta$

45-45-90

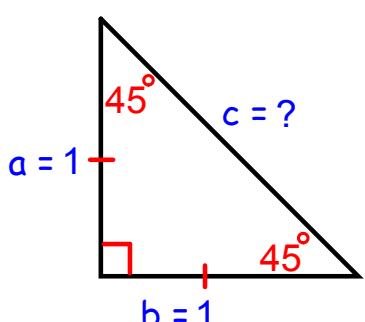


Hints...

- Give shortest side a convenient length
- Use Pythag Thm

## Side length ratios for a 45-45-90 $\Delta$

45-45-90



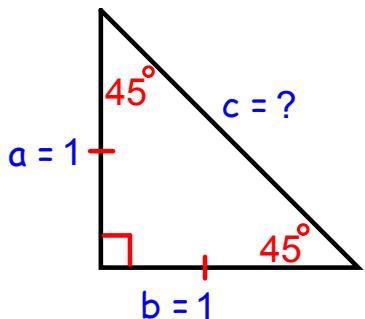
Hints...

- Give shortest side a convenient length
- Use Pythag Thm

$$c^2 = a^2 + b^2$$

## Side length ratios for a 45-45-90 $\Delta$

45-45-90



### Hints...

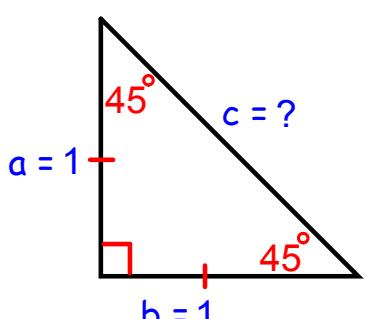
- Give shortest side a convenient length
- Use Pythag Thm

$$c^2 = a^2 + b^2$$

$$c^2 = 1^2 + 1^2$$

## Side length ratios for a 45-45-90 $\Delta$

45-45-90



### Hints...

- Give shortest side a convenient length
- Use Pythag Thm

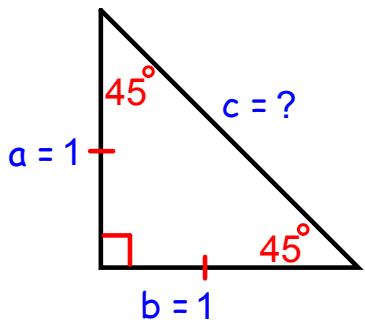
$$c^2 = a^2 + b^2$$

$$c^2 = 1^2 + 1^2$$

$$c^2 = 2$$

## Side length ratios for a 45-45-90 $\Delta$

45-45-90



### Hints...

- Give shortest side a convenient length
- Use Pythag Thm

$$c^2 = a^2 + b^2$$

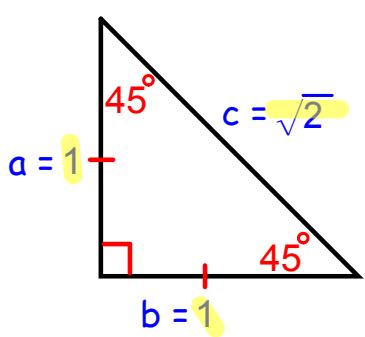
$$c^2 = 1^2 + 1^2$$

$$c^2 = 2$$

$$c = \sqrt{2}$$

## Side length ratios for a 45-45-90 $\Delta$

45-45-90



### Hints...

- Give shortest side a convenient length

- Use Pythag Thm

$$c^2 = a^2 + b^2$$

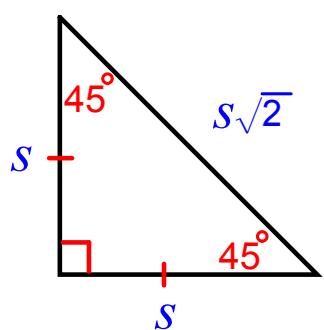
$$c^2 = 1^2 + 1^2$$

$$c^2 = 2$$

$$c = \sqrt{2}$$

## Thm 7-8: 45-45-90 Δ

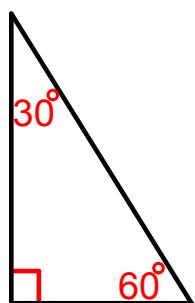
45-45-90



$$\text{hyp} = \sqrt{2} * \text{leg}$$

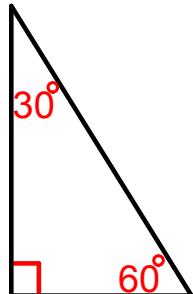
## Side length ratios for a 30-60-90 Δ

30-60-90



## Side length ratios for a 30-60-90 $\Delta$

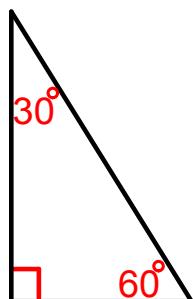
30-60-90



Hints...

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

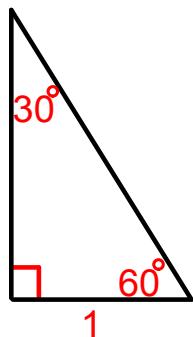


Hints...

- Give shortest side a convenient length

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

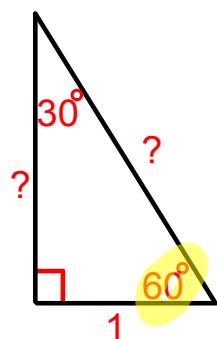


Hints...

- Give shortest side a convenient length

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

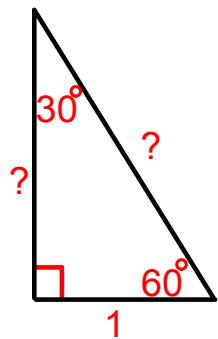


Hints...

- Give shortest side a convenient length

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

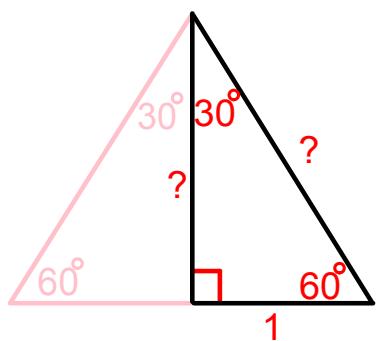


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

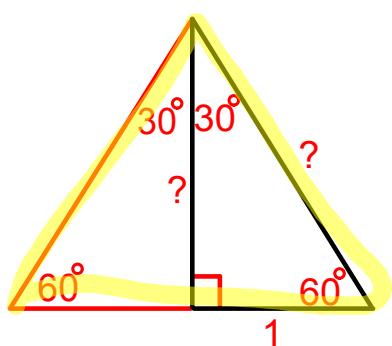


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

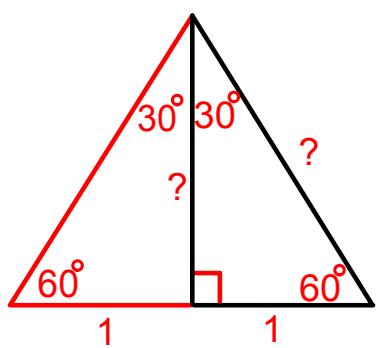


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

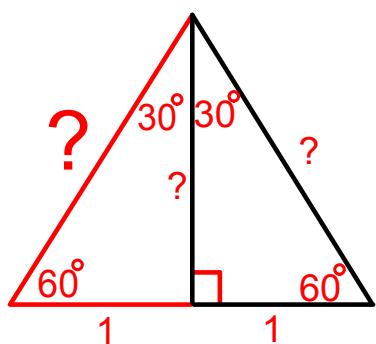


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

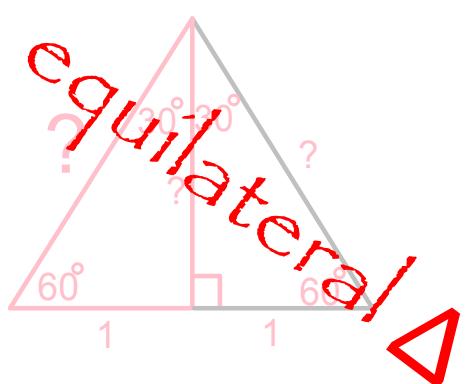


### Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

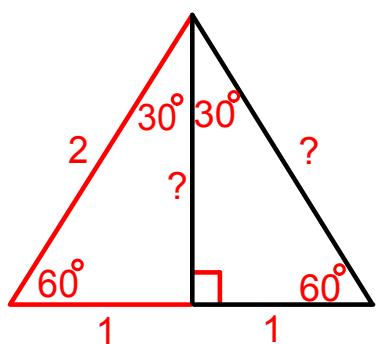


### Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

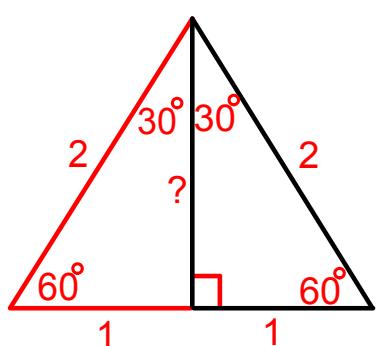


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

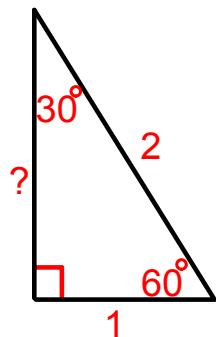


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

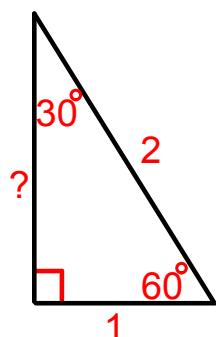


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

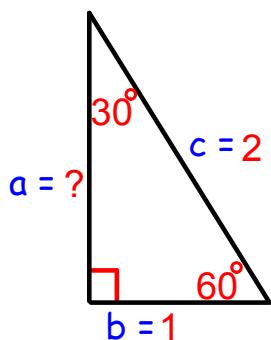


Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?
- Use Pythag Thm

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

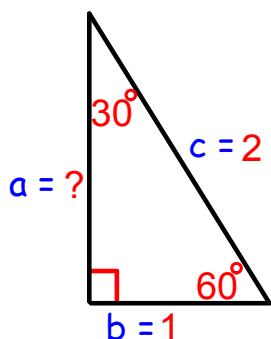


### Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?
- Use Pythag Thm

## Side length ratios for a 30-60-90 $\Delta$

30-60-90



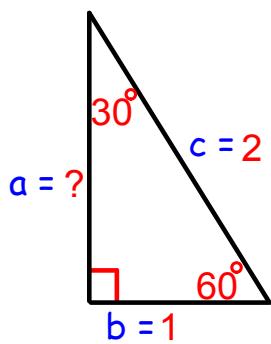
### Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?
- Use Pythag Thm

$$c^2 = a^2 + b^2$$

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

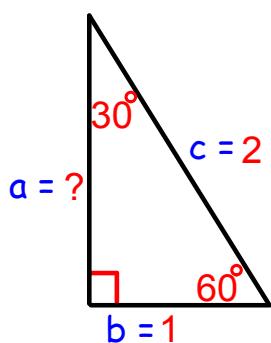


### Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?
- Use Pythag Thm  
 $c^2 = a^2 + b^2$   
 $2^2 = a^2 + 1^2$

## Side length ratios for a 30-60-90 $\Delta$

30-60-90

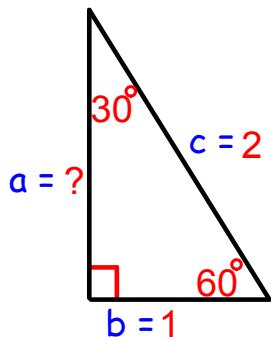


### Hints...

- Give shortest side a convenient length
- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?
- Use Pythag Thm  
 $c^2 = a^2 + b^2$   
 $2^2 = a^2 + 1^2$   
 $4 = a^2 + 1$

## Side length ratios for a 30-60-90 $\Delta$

30-60-90



Hints...

- Give shortest side a convenient length

- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

- Use Pythag Thm

$$c^2 = a^2 + b^2$$

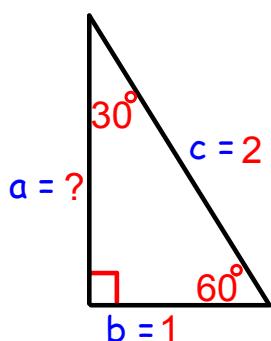
$$2^2 = a^2 + 1^2$$

$$4 = a^2 + 1$$

$$a^2 = 3$$

## Side length ratios for a 30-60-90 $\Delta$

30-60-90



Hints...

- Give shortest side a convenient length

- Is the 30-60-90  $\Delta$   $\frac{1}{2}$  of something?

- Use Pythag Thm

$$c^2 = a^2 + b^2$$

$$2^2 = a^2 + 1^2$$

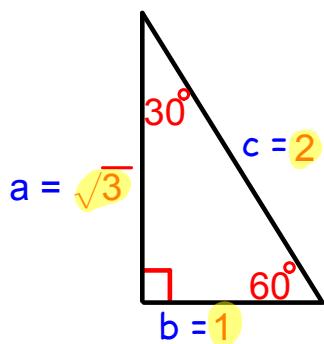
$$4 = a^2 + 1$$

$$a^2 = 3$$

$$a = \sqrt{3}$$

## Side length ratios for a 30-60-90 Δ

30-60-90



### Hints...

- Give shortest side a convenient length
- Is the 30-60-90 Δ  $\frac{1}{2}$  of something?
- Use Pythag Thm

$$c^2 = a^2 + b^2$$

$$2^2 = a^2 + 1^2$$

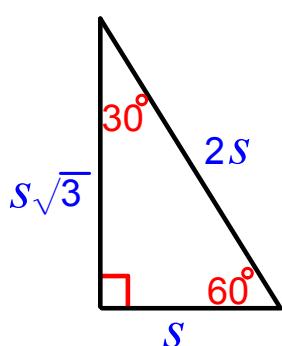
$$4 = a^2 + 1$$

$$a^2 = 3$$

$$a = \sqrt{3}$$

## Thm 7-9: 30-60-90 Δ

30-60-90



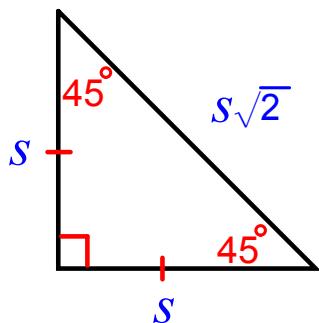
hyp = 2 \* shorter leg

longer leg =  $\sqrt{3}$  \* shorter leg

## The two special right triangles

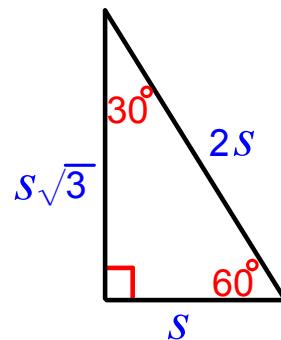
45-45-90

(Thm 7-8)



30-60-90

(Thm 7-9)



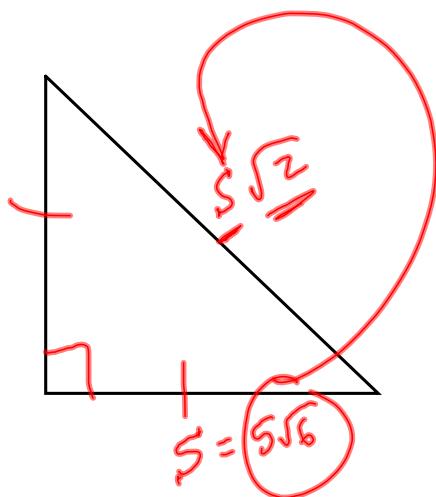
## Tips...

- Mental math is much faster than using a calculator.
- For these probs, answers almost always left in radical form.
- Do not leave a root/radical in the denominator of a fraction.
- First find shorter leg when working with a 30-60-90.

## Example 1

Find length of the hypotenuse of a 45-45-90  $\Delta$

w/legs of length  $5\sqrt{6}$ .

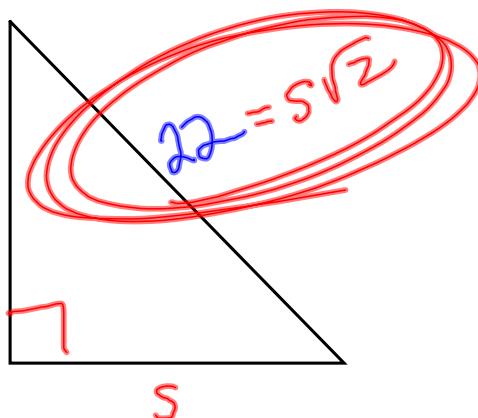


$$\begin{aligned}\sqrt{300} &= \sqrt{100 \cdot 3} \\ &= \sqrt{100} \cdot \sqrt{3} \\ &= 10\sqrt{3}\end{aligned}$$

$$\begin{aligned}s &\\ (5\sqrt{6})(\sqrt{2}) &\\ 5\sqrt{6}\sqrt{2} &= 5\sqrt{6 \cdot 2} \\ &= 5\sqrt{12} \\ &= 5\sqrt{4 \cdot 3} \\ &= 5 \cdot 2 \cdot \sqrt{3} \\ &= 10\sqrt{3}\end{aligned}$$

## Example 2

Find length of leg of a 45-45-90  $\Delta$  w/hypotenuse of length 22.



$$\begin{aligned}\frac{22}{\sqrt{2}} &= s\cancel{\sqrt{2}} \cancel{\sqrt{2}} \\ s &= \frac{22 \cdot \sqrt{2}}{\sqrt{2} \sqrt{2}} = \frac{22\sqrt{2}}{2} \\ &= 11\sqrt{2}\end{aligned}$$

### Example 3

The distance from 1 corner of a square playground to the opposite corner is 96ft. To the nearest foot, how long is each side of the playground?  $68'$

A diagram of a square playground. The top-left corner is shaded yellow. The side length is labeled  $s$ . The diagonal from the top-left corner to the bottom-right corner is labeled  $96 = \sqrt{2}s$ . The right angle at the bottom-left corner is marked with a square.

$$\frac{96}{\sqrt{2}} = \frac{s\sqrt{2}}{\sqrt{2}}$$
$$s = \frac{96}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{96\sqrt{2}}{2}$$
$$= 48\sqrt{2}$$
$$= 67.88225$$
$$\approx 68$$

### Example 4

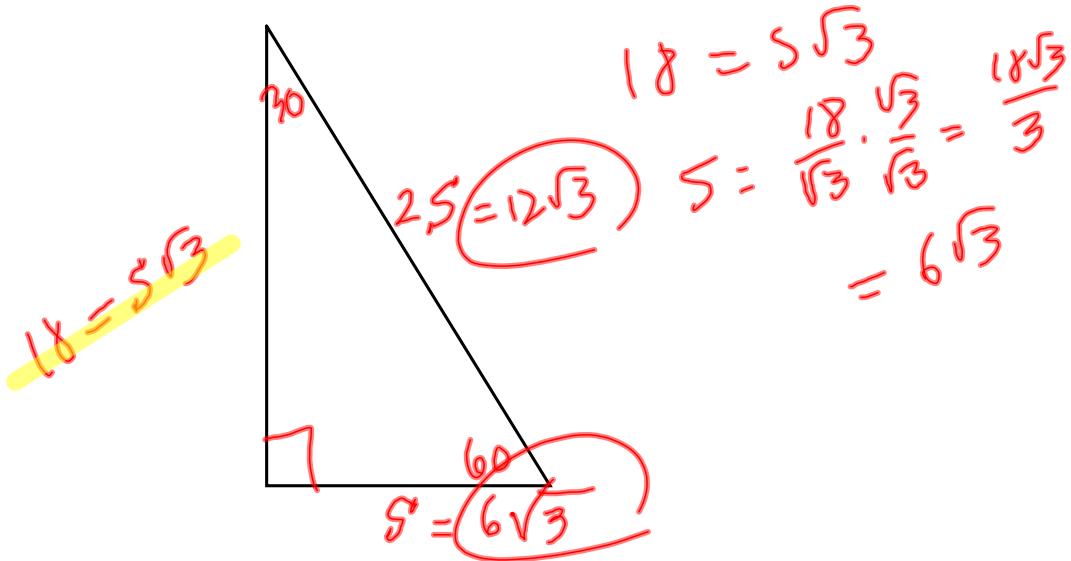
Find lengths of the legs of a 30-60-90  $\Delta$  w/ hypotenuse of length  $4\sqrt{3}$ .

A diagram of a 30-60-90 degree triangle. The top vertex is labeled 30, the bottom-left vertex is labeled 60, and the bottom-right vertex is labeled 90. The left leg is labeled  $2\sqrt{3}$ , the right leg is labeled  $s = 2\sqrt{3}$ , and the hypotenuse is labeled  $4\sqrt{3}$ . A yellow circle highlights the expression  $2\sqrt{3} = (2\sqrt{3})(\sqrt{3})$ .

$$\frac{2\sqrt{3}}{2} = \frac{4\sqrt{3}}{2}$$
$$s = 2\sqrt{3}$$
$$2\sqrt{3} = (2\sqrt{3})(\sqrt{3})$$
$$2 \cdot 3 = 6$$

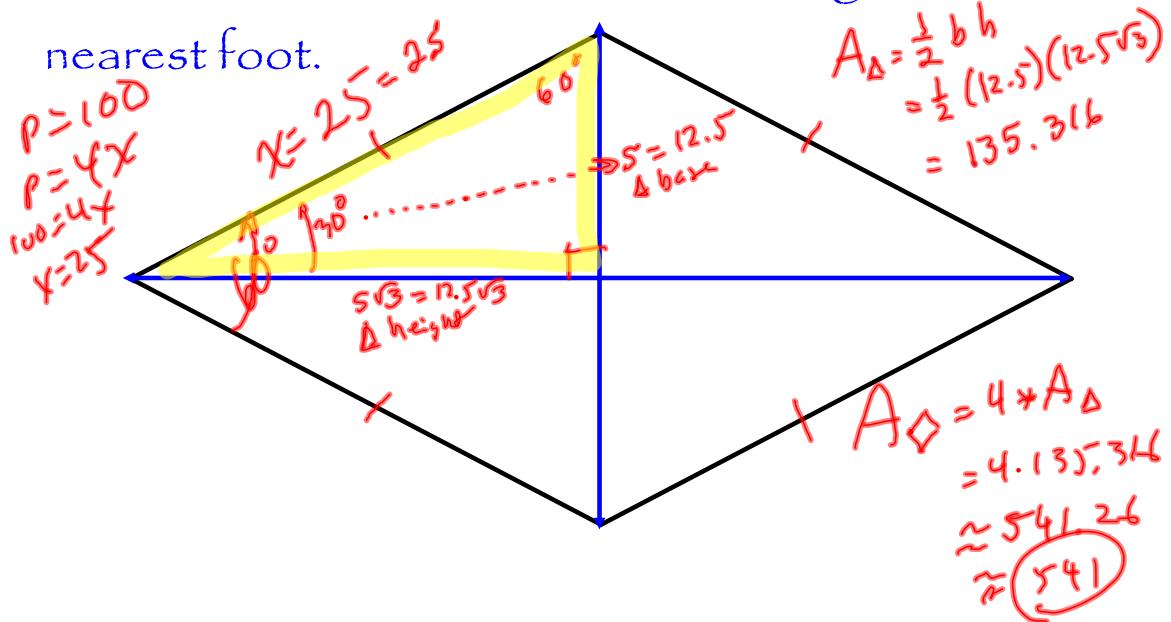
## Example 5

The longer leg of a 30-60-90 has length 18. Find the lengths of the shorter leg and hypotenuse.



## Example 6

A garden shaped like a rhombus has a perimeter of 100ft & a  $60^\circ$  angle. Find the area of the garden to the nearest foot.



## L7-3 HW Problems

Pg 369 #1-29, 32, 33-39

Pg 372 #1-10